
PUMPE

ZAKON SLIČNOSTI I DIMENZIJSKA ANALIZA

DIMENZIJSKA ANALIZA OSNOVNIH PARAMETARA

Dimenzijskom analizom organiziramo veličine koje utječu na rad pumpe:

- ρ -gustoća vode [kg/m^3],
- ω -kutna brzina vrtnje rotora [rad/s],
- D -promjer kola rotora [m],
- Δp -prirast tlaka kroz pumpu [Pa],
- Q -protok vode kroz pumpu [m^3/s],
- P -snaga pumpe [W].

BEZDIMENZIJSKI PARAMETRI

Bezdimenzijska specifična energija

$$\psi = \Pi_1 = \frac{\Delta p}{\rho \omega^2 D^2} = \frac{gH}{\omega^2 D^2}$$

Bezdimenzijski protok

$$\varphi = \Pi_2 = \frac{Q}{\omega \cdot D^3}$$

Bezdimenzijska snaga

$$C_P = \frac{P}{\rho \cdot \omega^3 \cdot D^5}$$

Efikasnost

$$\eta = \frac{\Delta p \cdot Q}{P} = \frac{\psi \cdot \varphi}{C_P}$$

BEZDIMENZIJSKI BROJ OKRETAJA - BRZOHODNOST

$$C_{\omega} = \Pi_4 = \frac{\omega \cdot \sqrt{Q}}{\left(\frac{\Delta p}{\rho}\right)^{3/4}} = \frac{\sqrt{\varphi}}{\psi^{3/4}}$$

ZAKON SLIČNOSTI

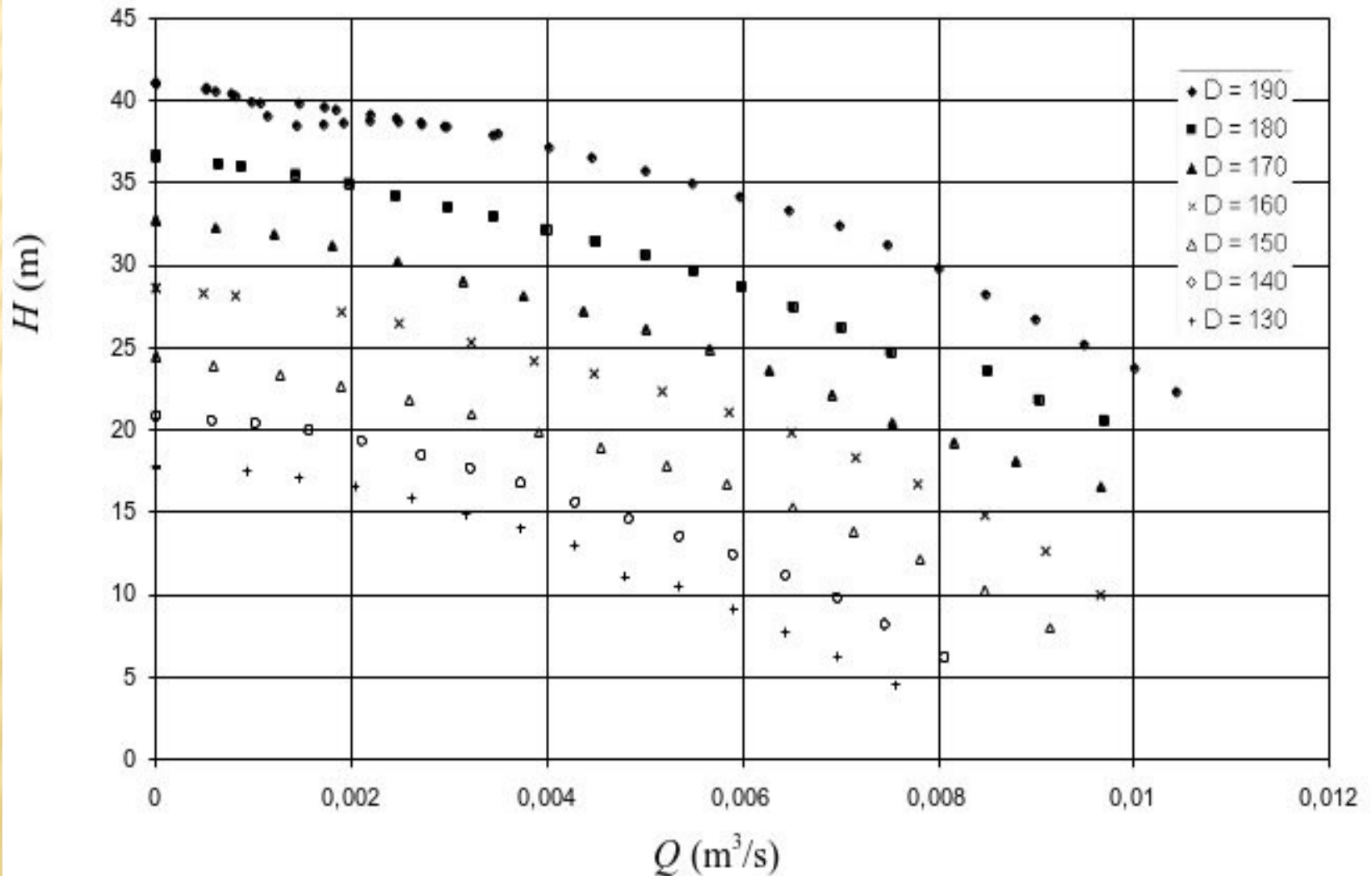
Rad pumpi je definiran bezdimenzijskim krivuljama

$$\psi = f(\varphi) \quad \text{i} \quad C_p = f(\varphi)$$

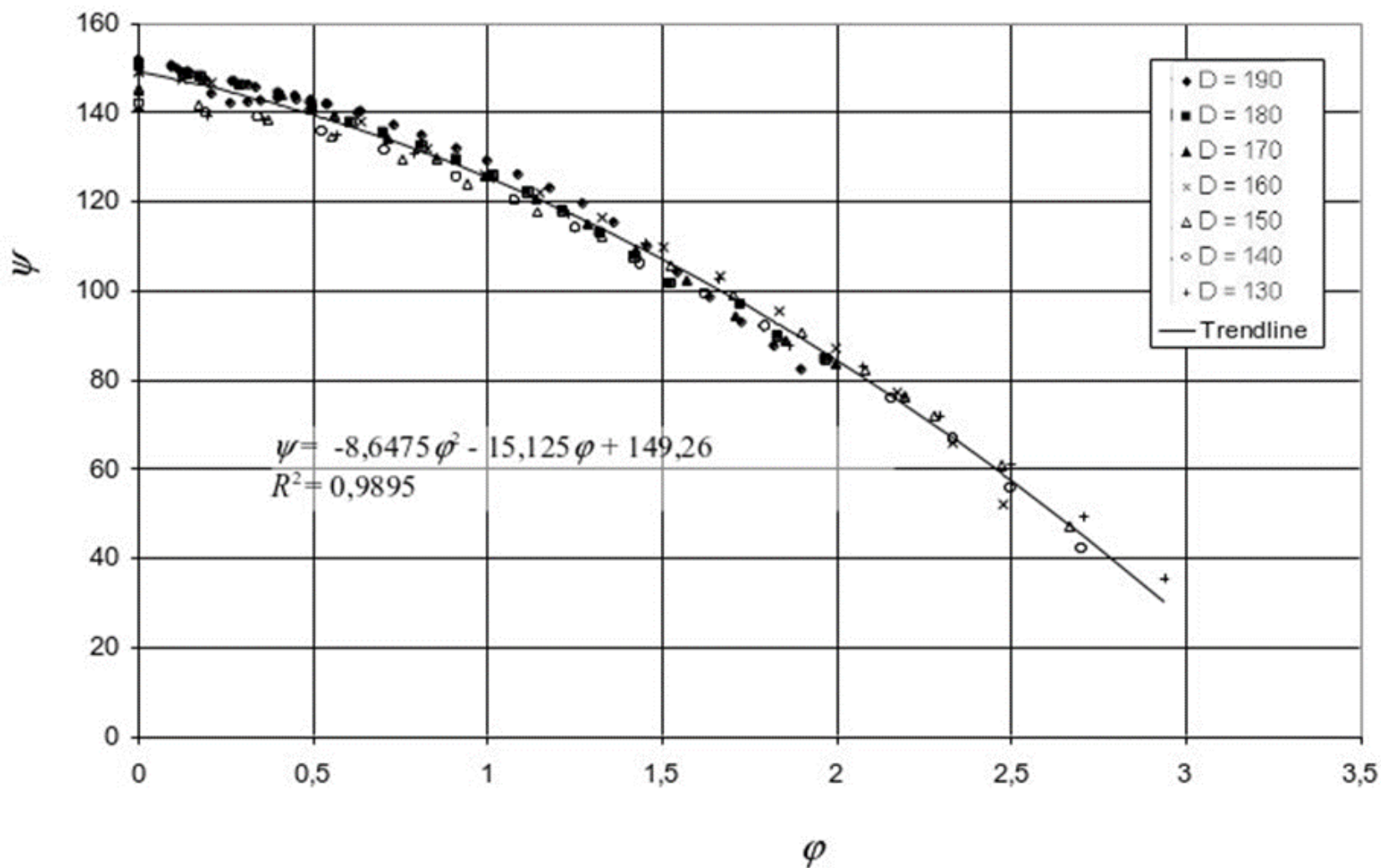
Dvije slične pumpe moraju:

1. biti geometrijski slične
2. imati iste sve bezdimenzijske krivulje

JEDINSTVO IB - SERIJA



JEDINSTVO IB BEZDIMENZIJSKE KARAKTERISTIKE



ZAKON SLIČNOSTI

□ Kada dvije slične pumpe rade u istoj radnoj točki to znači da su im i π parametri isti. Sva tri bezdimenzijska parametra (visina dobave, protok i snaga) moraju biti isti za obje slične pumpe.

$$\psi = \frac{\Delta p_1}{\rho_1 \omega_1^2 D_1^2} = \frac{\Delta p_2}{\rho_2 \omega_2^2 D_2^2}$$

$$\varphi = \frac{Q_1}{\omega_1 \cdot D_1^3} = \frac{Q_2}{\omega_2 \cdot D_2^3}$$

$$C_P = \frac{P_1}{\rho_1 \cdot \omega_1^3 \cdot D_1^5} = \frac{P_2}{\rho_2 \cdot \omega_2^3 \cdot D_2^5}$$

ZAKON SLIČNOSTI – SPECIFIČNI SLUČAJ

Specijalni slučaj –pumpa radi s istim fluidom ali na raznom broju okretaja

$$\psi = \frac{\Delta p_1}{\rho_1 \omega_1^2 D_1^2} = \frac{\Delta p_2}{\rho_2 \omega_2^2 D_2^2}$$

$$\varphi = \frac{Q_1}{\omega_1 \cdot D_1^3} = \frac{Q_2}{\omega_2 \cdot D_2^3}$$

$$C_P = \frac{P_1}{\rho_1 \cdot \omega_1^3 \cdot D_1^5} = \frac{P_2}{\rho_2 \cdot \omega_2^3 \cdot D_2^5}$$

$$\frac{\Delta p_1}{\Delta p_2} = \frac{\omega_1^2}{\omega_2^2}$$

$$\frac{Q_1}{Q_2} = \frac{\omega_1}{\omega_2}$$

$$\frac{P_1}{P_2} = \frac{\omega_1^3}{\omega_2^3}$$

SLIČNOST PUMPI– ISTI FLUID I ISTA PUMPA

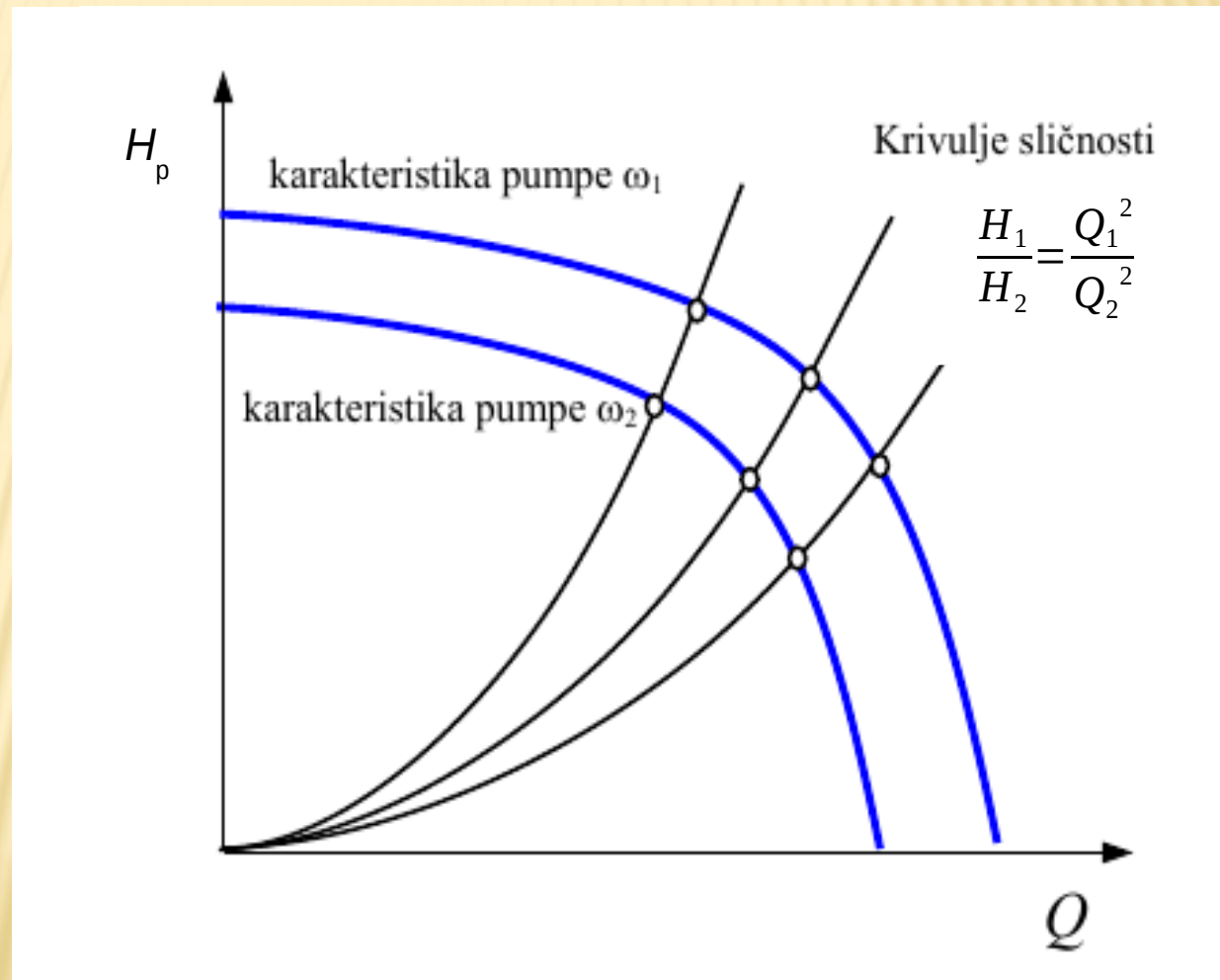
$$\frac{\Delta p_1}{\Delta p_2} = \frac{\omega_1^2}{\omega_2^2}$$

$$\frac{Q_1}{Q_2} = \frac{\omega_1}{\omega_2}$$

$$\frac{P_1}{P_2} = \frac{\omega_1^3}{\omega_2^3}$$

$$\frac{\Delta p_1}{\Delta p_2} = \frac{H_1}{H_2} = \frac{Q_1^2}{Q_2^2}$$

$$\frac{P_1}{P_2} = \frac{Q_1^3}{Q_2^3}$$



ZAKON SLIČNOSTI – SPECIFIČNI SLUČAJ

Specijalni slučaj – slične pumpe rade s istim fluidom i na istom broju okretaja

$$\begin{aligned} \psi &= \frac{\Delta p_1}{\rho_1 \omega_1^2 D_1^2} = \frac{\Delta p_2}{\rho_2 \omega_2^2 D_2^2} & \frac{\Delta p_1}{\Delta p_2} &= \frac{D_1^2}{D_2^2} \\ \varphi &= \frac{Q_1}{\omega_1 \cdot D_1^3} = \frac{Q_2}{\omega_2 \cdot D_2^3} & \frac{Q_1}{Q_2} &= \frac{D_1^3}{D_2^3} \\ C_P &= \frac{P_1}{\rho_1 \cdot \omega_1^3 \cdot D_1^5} = \frac{P_2}{\rho_2 \cdot \omega_2^3 \cdot D_2^5} & \frac{P_1}{P_2} &= \frac{D_1^5}{D_2^5} \end{aligned}$$

SLIČNOST PUMPI- ISTI FLUID I BROJ OKRETAJA

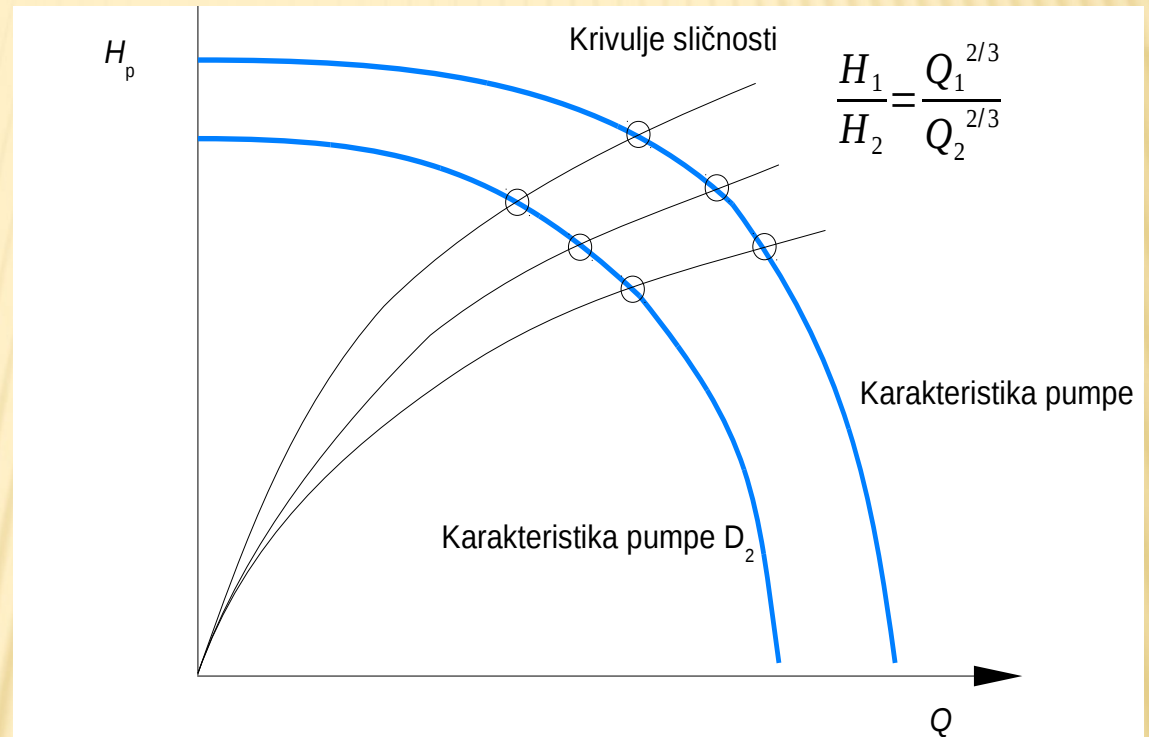
$$\frac{\Delta p_1}{\Delta p_2} = \frac{D_1^2}{D_2^2}$$

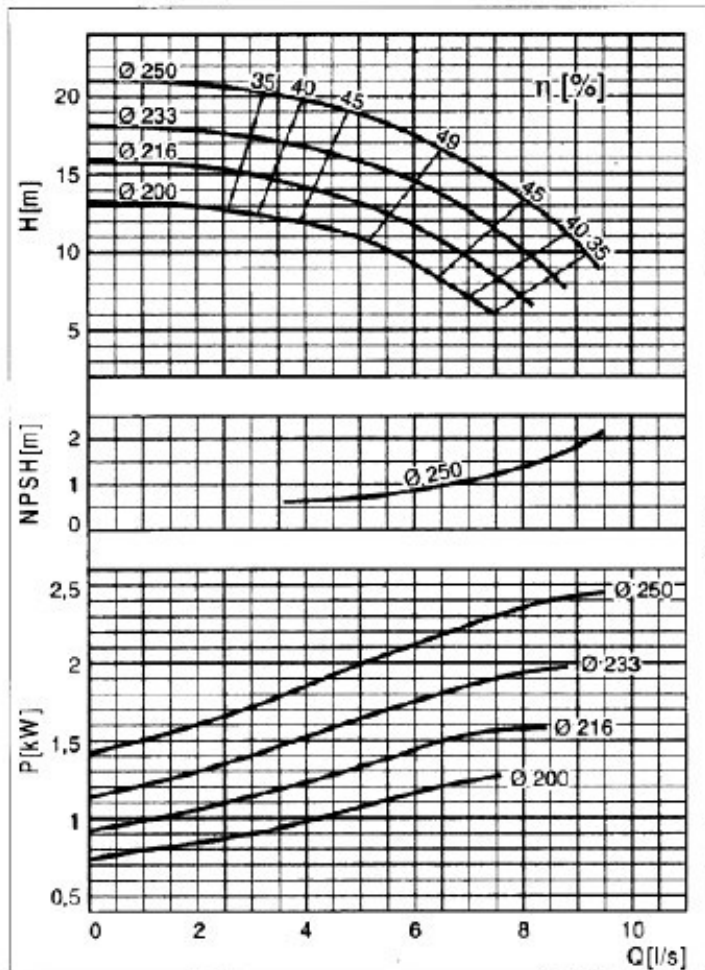
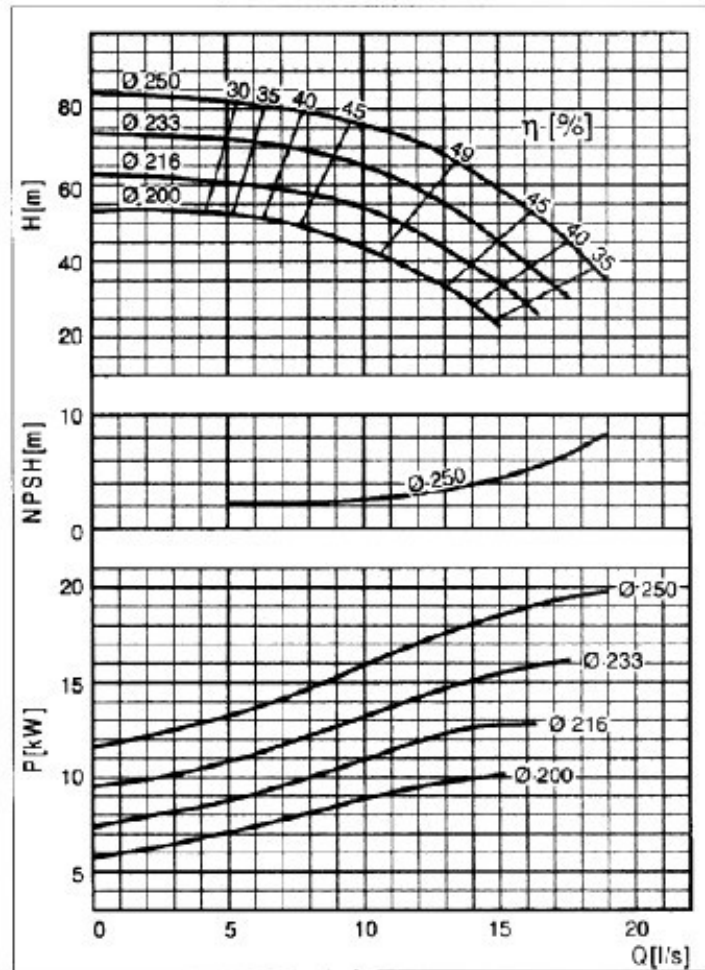
$$\frac{Q_1}{Q_2} = \frac{D_1^3}{D_2^3}$$

$$\frac{P_1}{P_2} = \frac{D_1^5}{D_2^5}$$

$$\frac{\Delta p_1}{\Delta p_2} = \frac{H_1}{H_2} = \frac{Q_1^{2/3}}{Q_2^{2/3}}$$

$$\frac{P_1}{P_2} = \frac{Q_1^{5/3}}{Q_2^{5/3}}$$

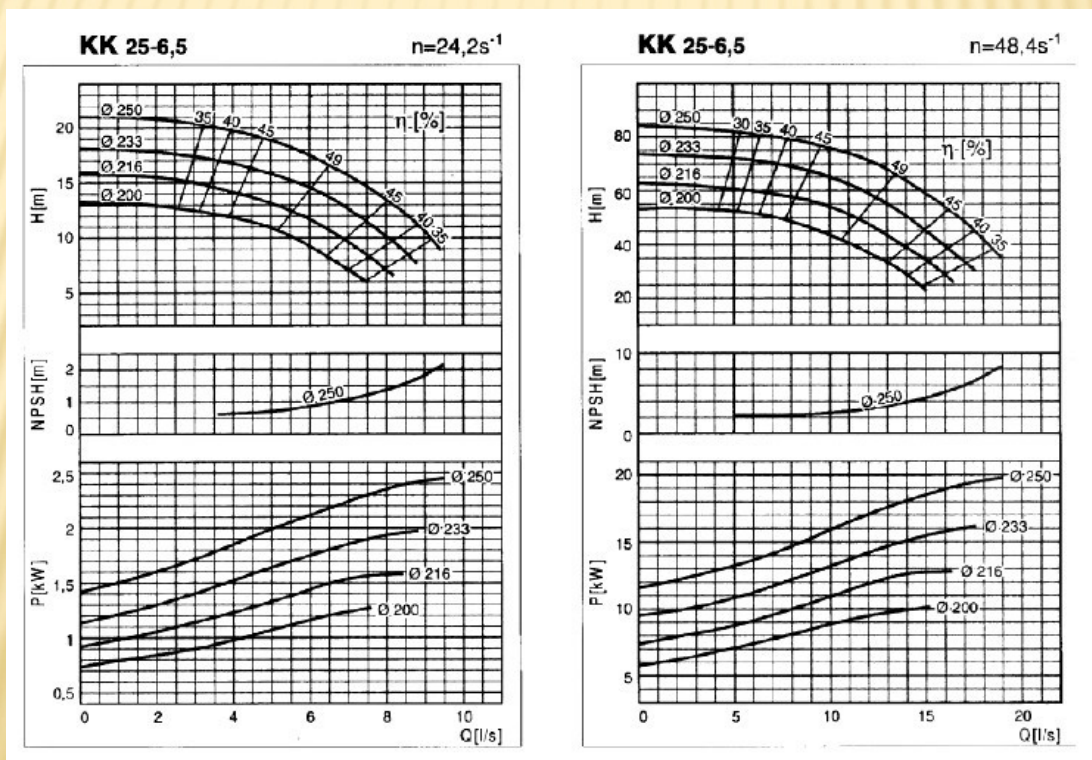


KK 25-6,5 $n=24,2\text{s}^{-1}$ **KK 25-6,5** $n=48,4\text{s}^{-1}$ 

ENERGETSKE KARAKTERISTIKE PUMPE

ENERGETSKE KARAKTERISTIKE PUMPE

- Visina dobave u zavisnosti o protoku,
- Snaga u ovisnosti o protoku,
- Efikasnost u ovisnosti o protoku,
- Neto pozitivna usisna visina u ovisnosti o protoku.

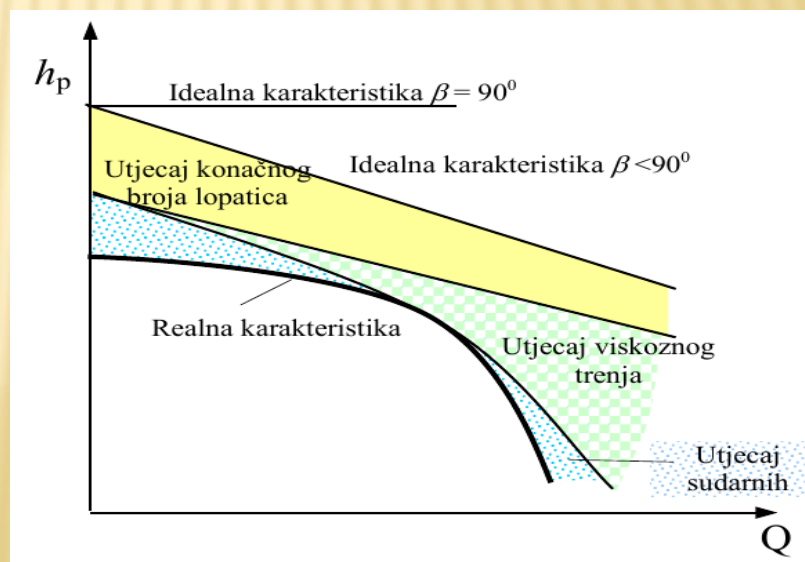
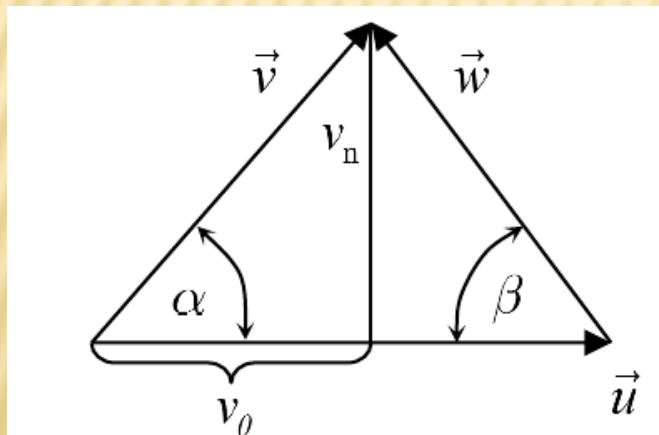


EULEROVE JEDNADŽBE ZA TURBOSTROJEVE

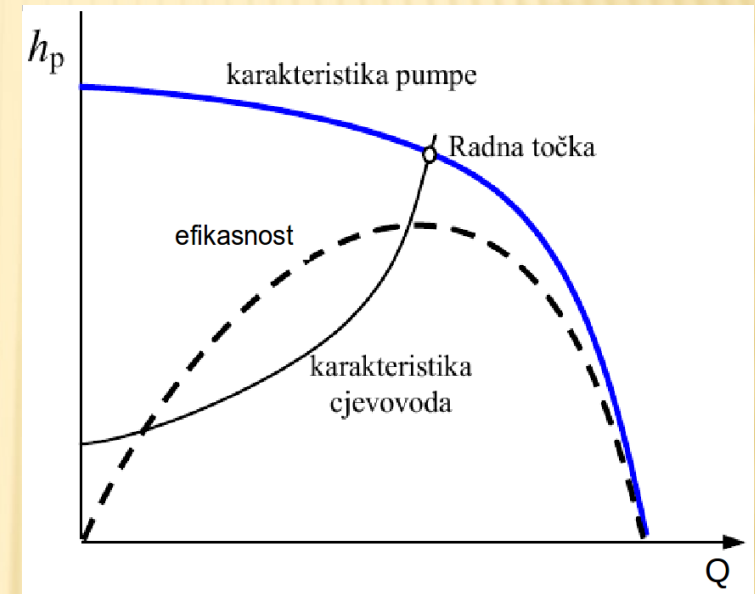
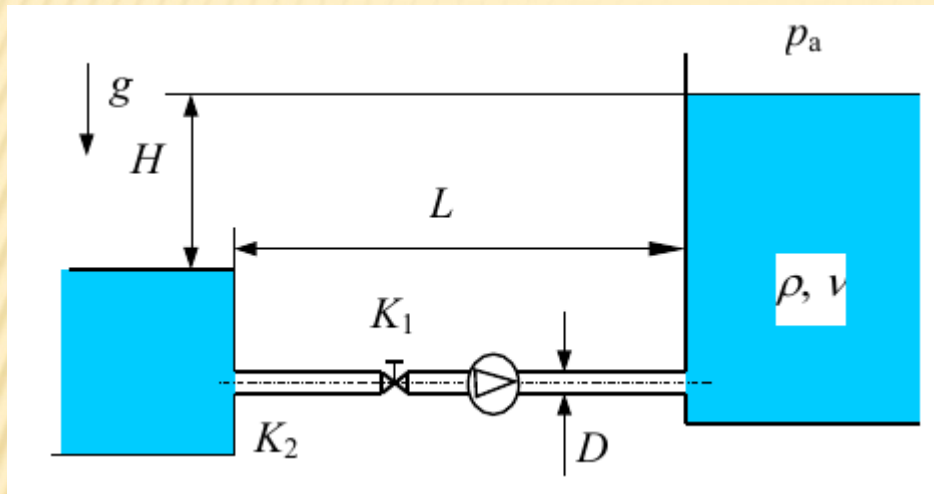
$$h_p = \frac{1}{g} (u_2 v_{2\theta} - u_1 v_{1\theta})$$

$$h_p = \frac{1}{g} \left(u_2 \underbrace{v_{2\theta}}_{(u_2 - w_2 \cos(\beta))} - u_1 \underbrace{v_{1\theta}}_0 \right) = \frac{1}{g} (u_2 (u_2 - w_2 \cos \beta))$$

$$h_p = \frac{1}{g} \left(\omega_2 r_2 \left(\omega_2 r_2 - \frac{Q}{A} \cos \beta \right) \right) = \frac{1}{g} \left(\omega_2^2 r_2^2 - \omega_2 r_2 \frac{Q}{A} \cos \beta \right)$$



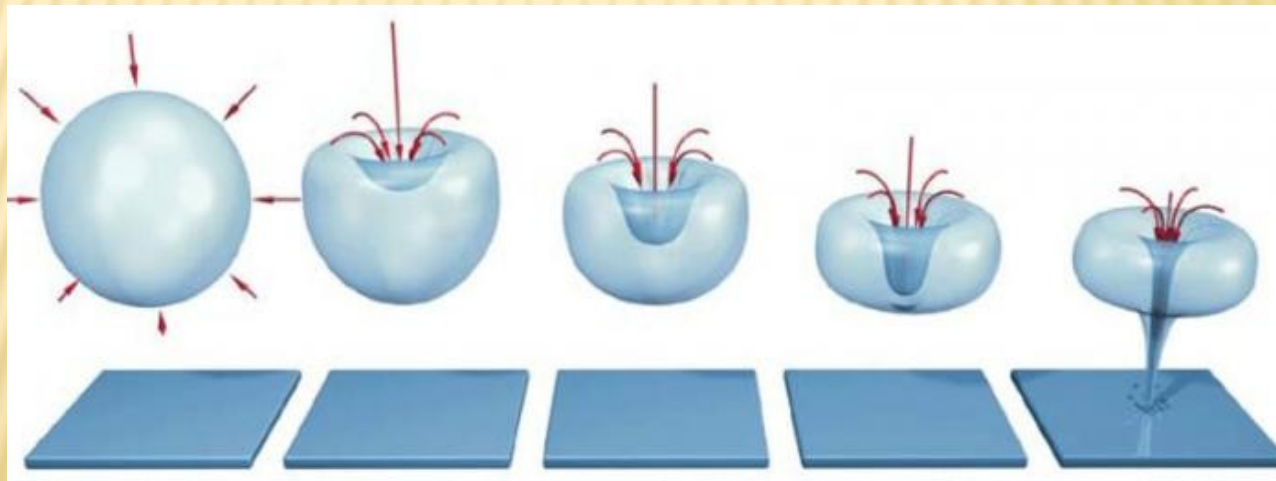
RADNA TOČKA



$$h_p = H + \lambda \frac{L}{D} \frac{8Q^2}{D^4 \pi^2 g} + K_1 \frac{8Q^2}{D^4 \pi^2 g} + K_2 \frac{8Q^2}{D^4 \pi^2 g} + \frac{8Q^2}{D^4 \pi^2 g}$$

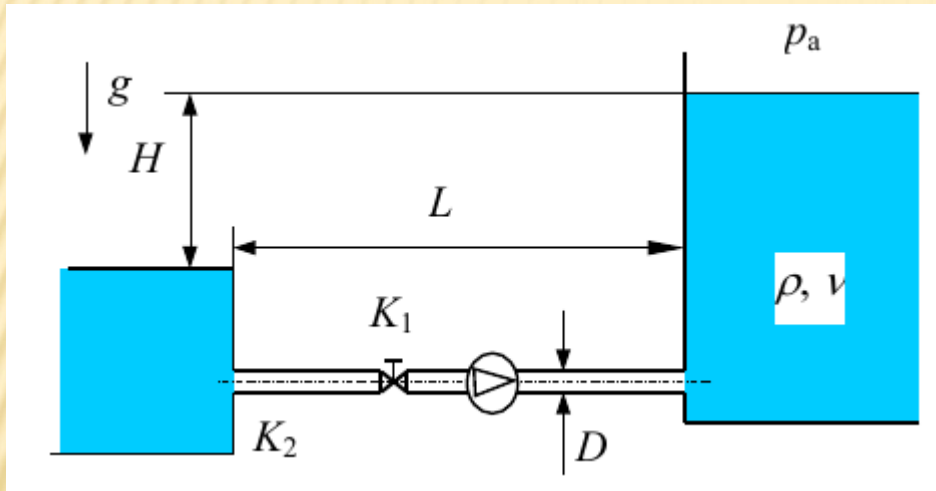
$$h_p = H + \left(\lambda \frac{L}{D} \frac{8}{D^4 \pi^2 g} + K_1 \frac{8}{D^4 \pi^2 g} + K_2 \frac{8}{D^4 \pi^2 g} + \frac{8}{D^4 \pi^2 g} \right) Q^2 = H + K \cdot Q^2$$

KAVITACIJA



RASPOLOŽIVA NETO POZITIVNA USISNA VISINA

Net Positive Suction Head Available



$$NPSH = H_t - \frac{p_v}{\rho g}$$

gdje je H_t totalni tlak na ulazu u pumpu,
a p_v tlak zasićenja.

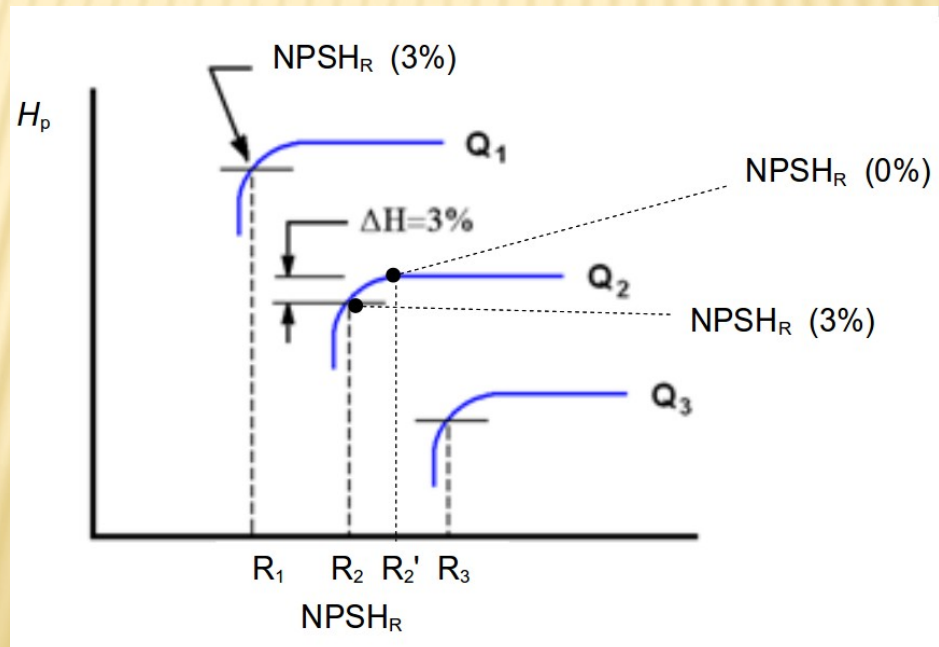
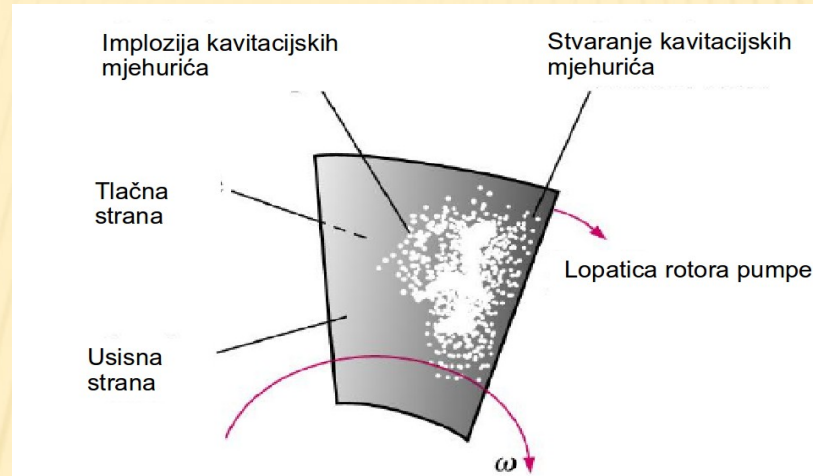
$$\frac{p_a}{\rho g} + \frac{v_1^2}{2g} + z_1 = \frac{p_2}{\rho g} + \frac{v_2^2}{2g} + z_2 + \lambda \frac{L_u}{D} \frac{v^2}{2g} + (K_1 + K_2) \frac{v^2}{2g}$$

$$\frac{p_a}{\rho g} + \frac{v_1^2}{2g} + z_1 - \lambda \frac{L_u}{D} \frac{v^2}{2g} - (K_1 + K_2) \frac{v^2}{2g} = \frac{p_2}{\rho g} + \frac{v_2^2}{2g} + z_2 = H_t = NPSH_A + \frac{p_v}{\rho g}$$

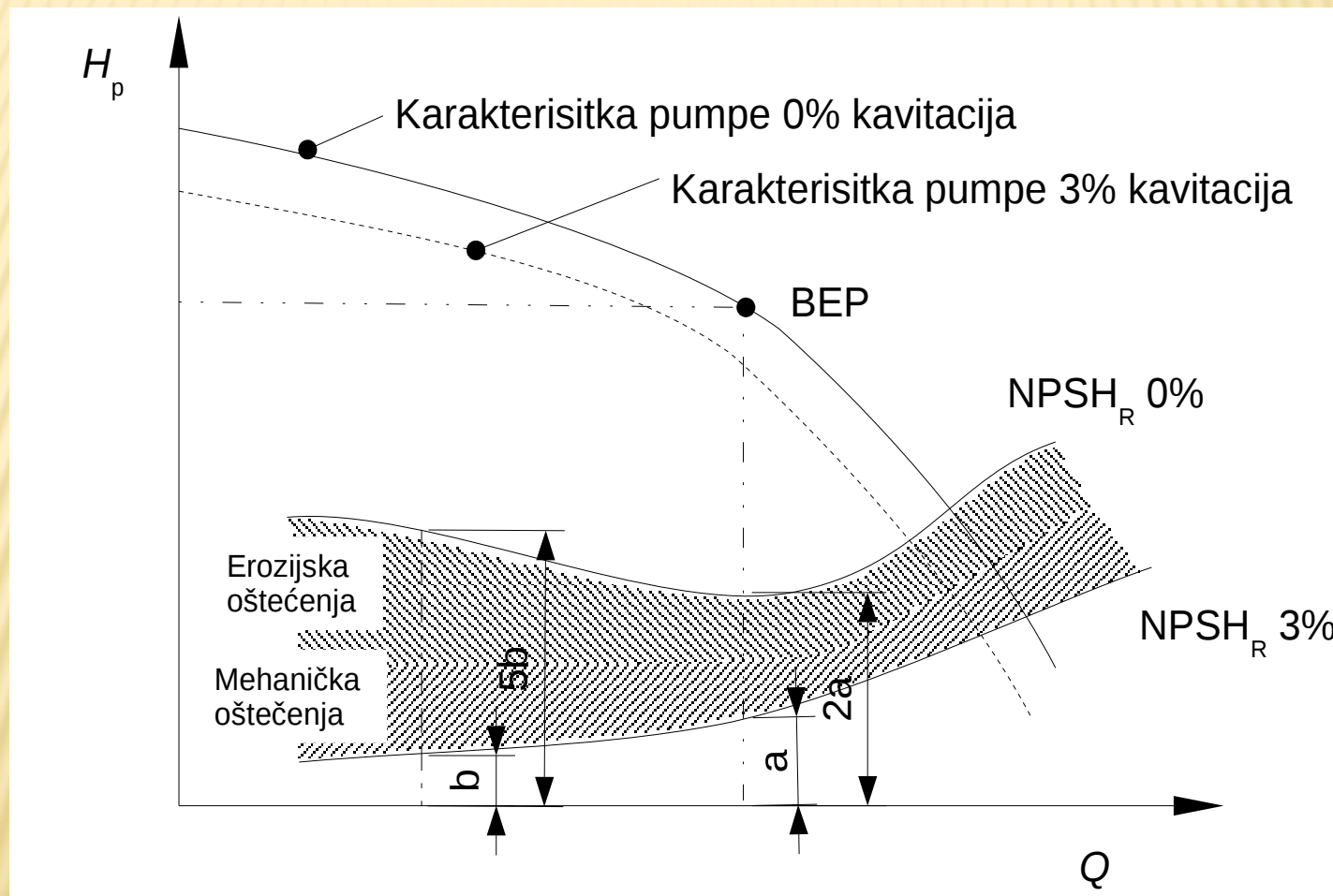
$$\frac{p_a}{\rho g} + \frac{v_1^2}{2g} + z_1 - \lambda \frac{L_u}{D} \frac{v^2}{2g} - (K_1 + K_2) \frac{v^2}{2g} > \frac{p_v}{\rho g}$$

$$NPSH_A = H_t - \frac{p_v}{\rho g}$$

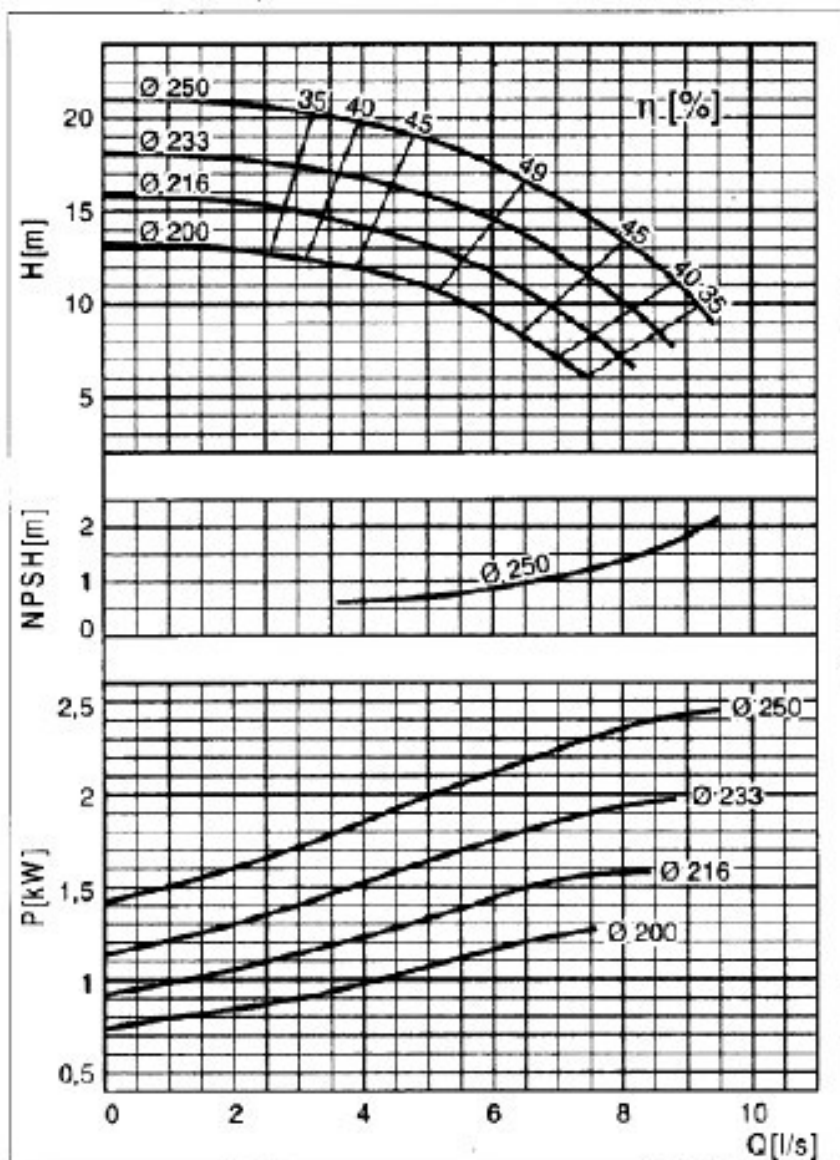
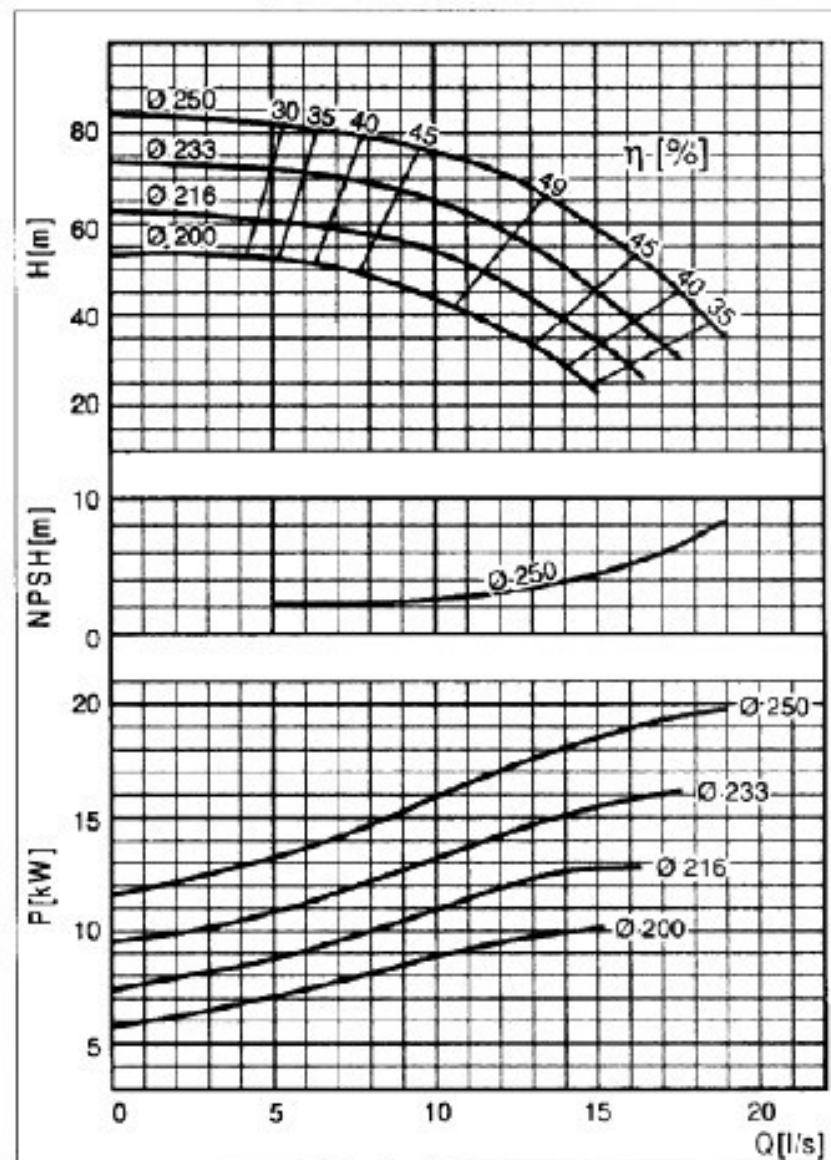
POTREBNA NETO POZITIVNA USISNA VISINA



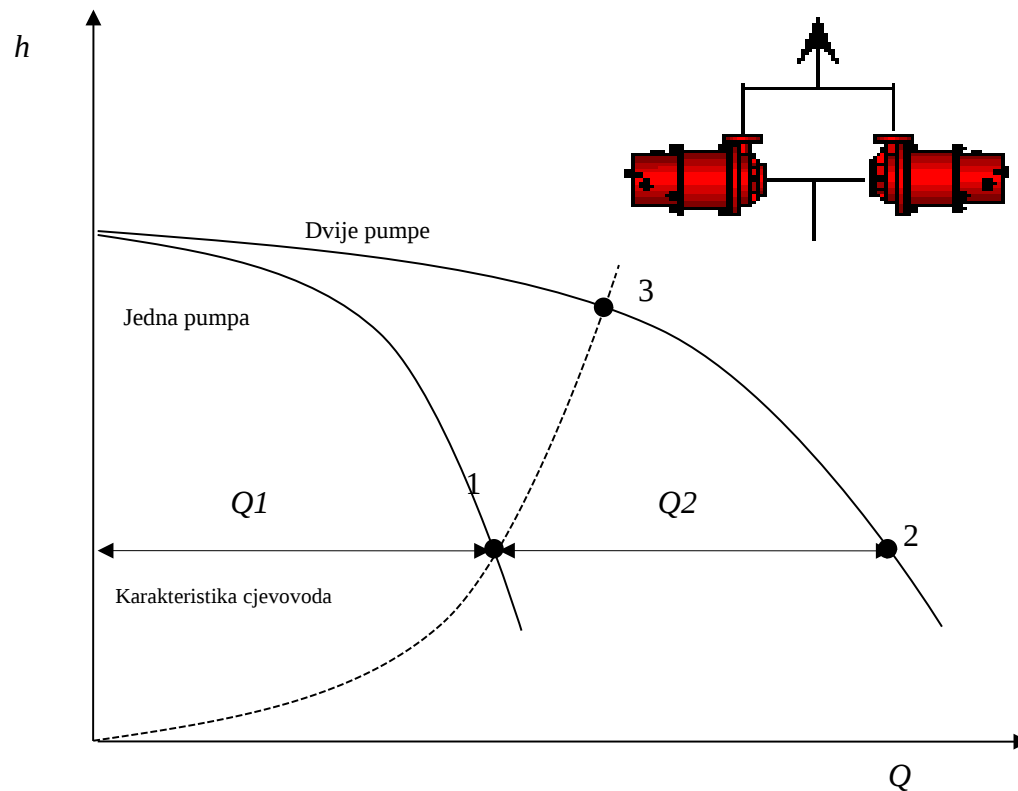
NPSH ZA 0% I 3% PADA VISINE DOBAVE



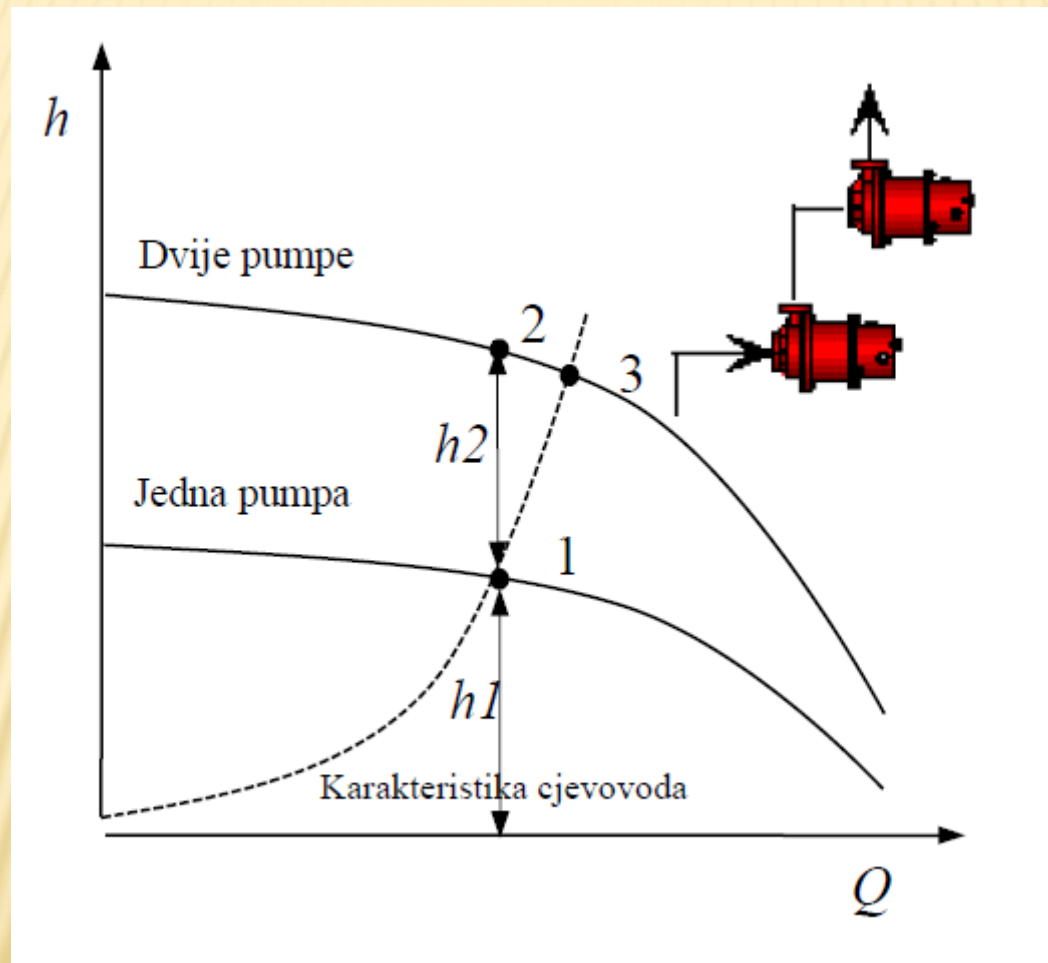
$$NPSH_A > NPSH_R$$

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PARALELNI RAD PUMPI

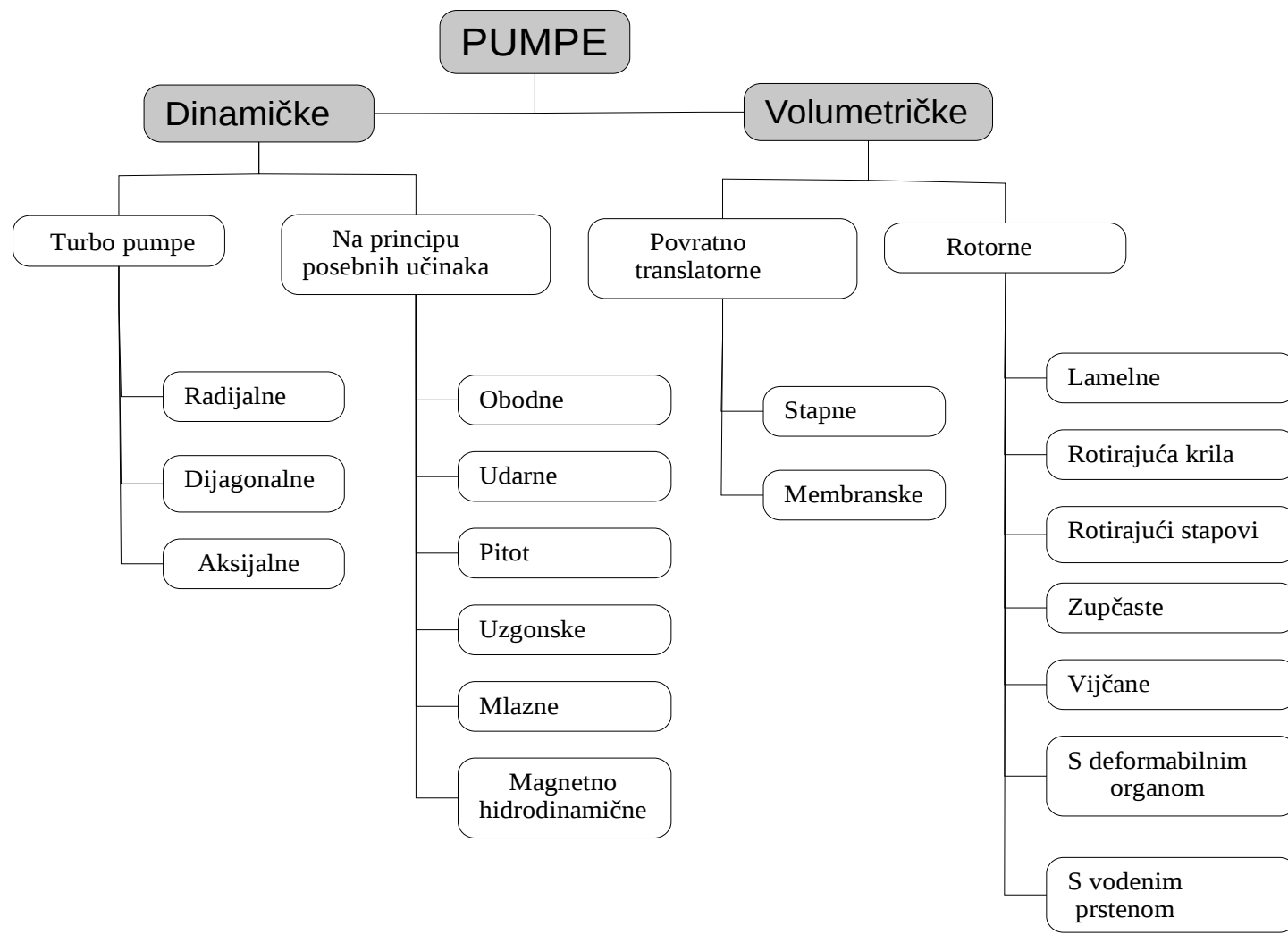


SERIJSKI RAD PUMPI



TIPOVI PUMPI

PODJELA PUMPI



BRZOHODNOST

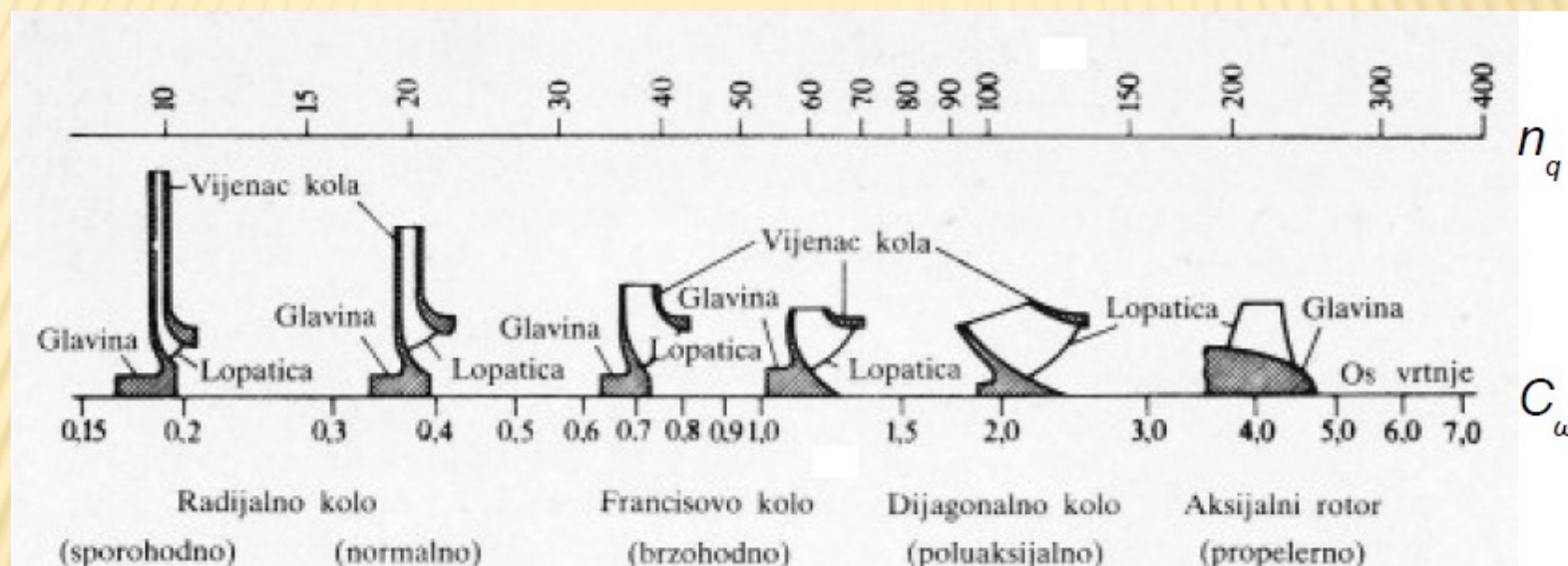
$$C_{\omega} = \frac{\omega \cdot \sqrt{Q}}{\left(\frac{\Delta p}{\rho}\right)^{3/4}} = \frac{\omega \cdot \sqrt{Q}}{(g \cdot H)^{3/4}} \quad n_q = \frac{n \cdot \sqrt{Q}}{(H)^{3/4}} \quad n_q = 52.919 \cdot C_{\omega}$$

gdje je n_q specifična brzina vrtnje u okretajima u minuti, n broj okretaja osovine u okretajima u minuti, Q metrima kubnim po satu, H u metrima.

$$N_s = \frac{n \cdot \sqrt{Q}}{(H)^{3/4}} \quad N_s = 2733.016 \cdot C_{\omega}$$

gdje je N_s specifična brzina vrtnje u okretajima u minuti, n broj okretaja osovine u okretajima u minuti, Q galoni u minuti, H u stopama

BRZOHODNOST



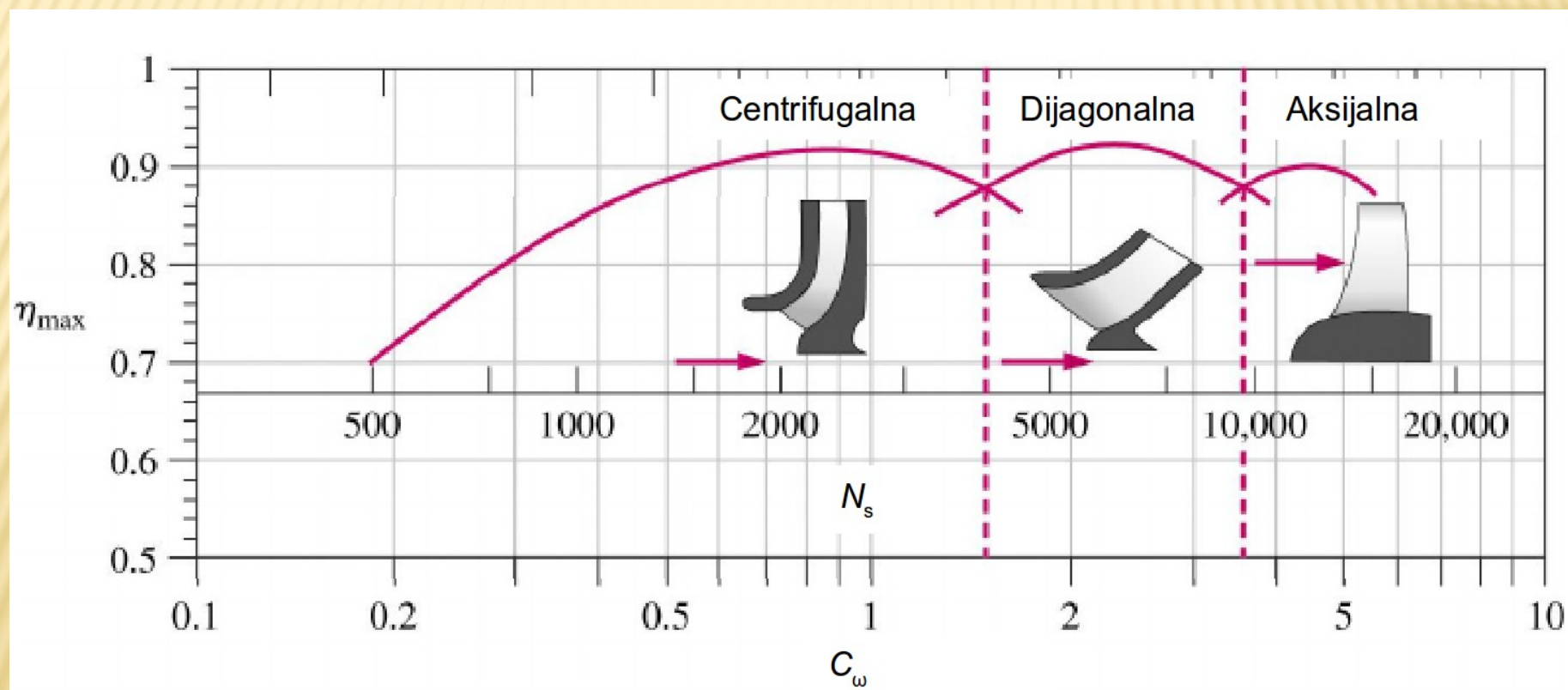
Centrifugalni rotor

Francis rotor

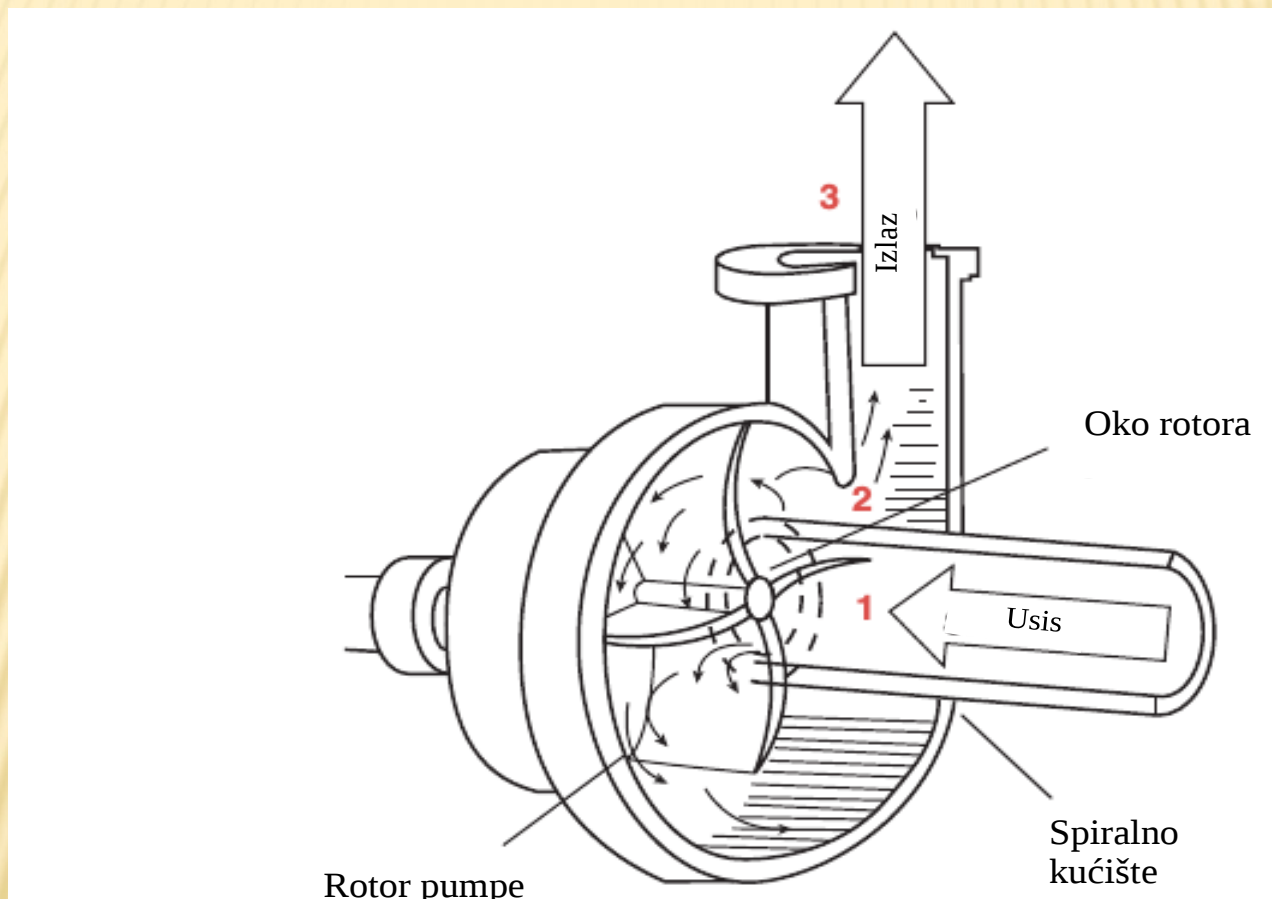
Dijagonalni rotor

Propelearni rotor

BRZOHODNOST



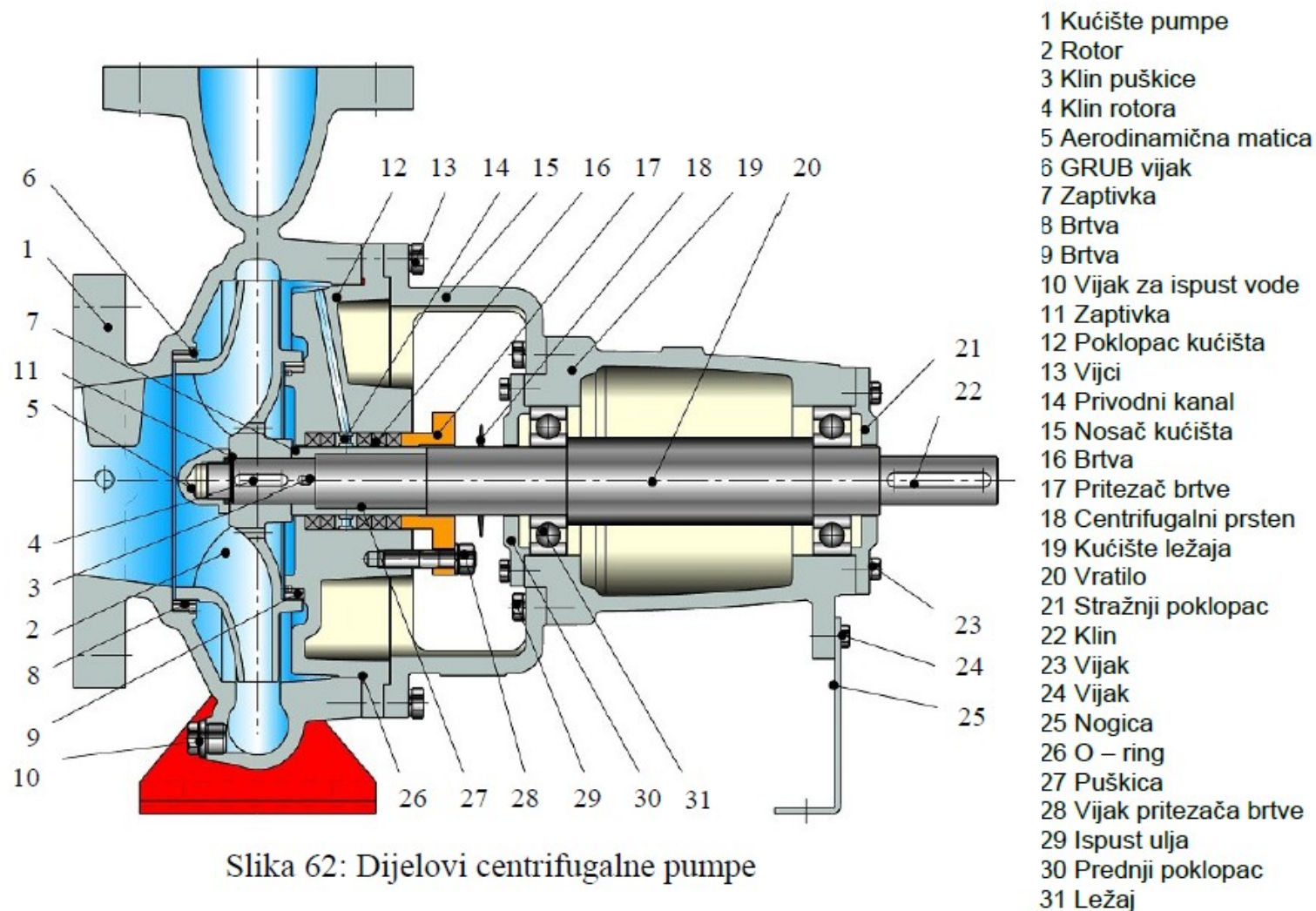
IZGLED PUMPE I GLAVNI DJELOVI



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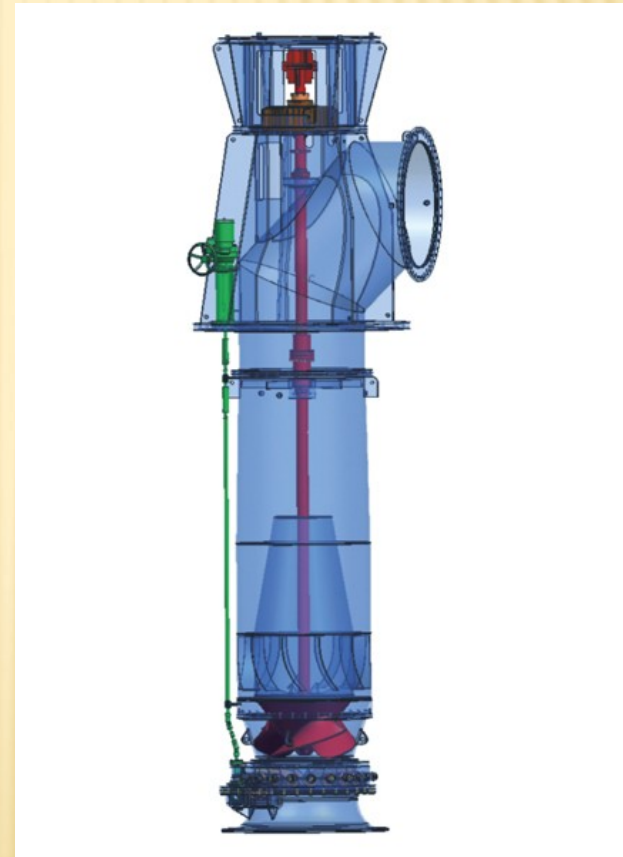
IZGLED PUMPE I GLAVNI DJELOVI



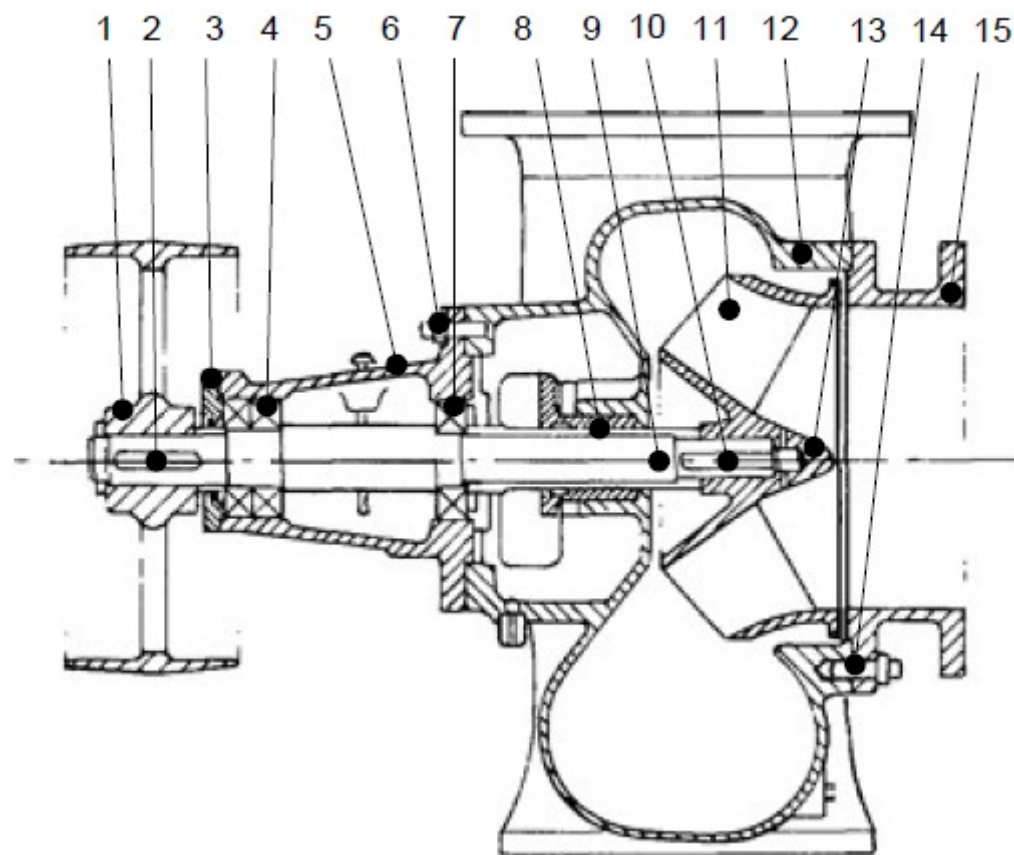
ROTOR CENTRIFUGALNE PUMPE



DIJAGONALNA PUMPA

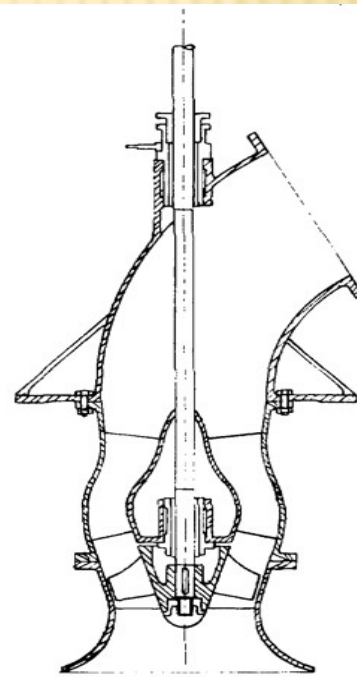
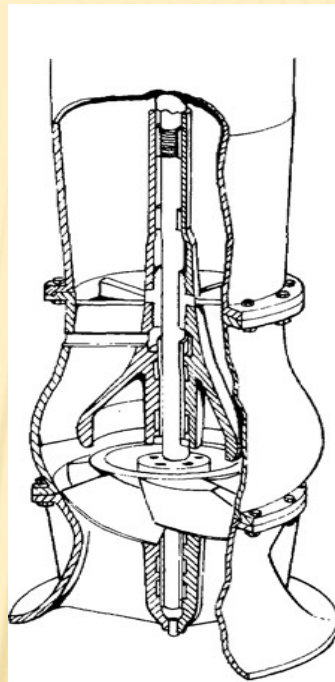
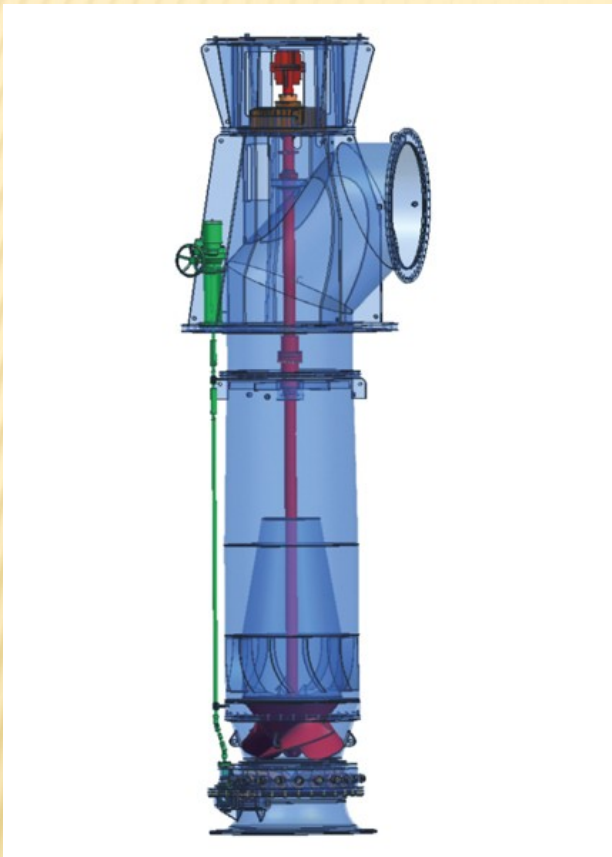


DIJAGONALNA PUMPA



- 1 Remenica
- 2 Klin remenice
- 3 Stražnji poklopac
- 4 Ležaj
- 5 Kućište ležaja
- 6 Vijak
- 7 Ležaj
- 8 Brtva
- 9 Osovina
- 10 Klin rotora
- 11 Rotor
- 12 Kućište
- 13 Aerodinamična matica
- 14 Vijak
- 15 Prirubnica usisna

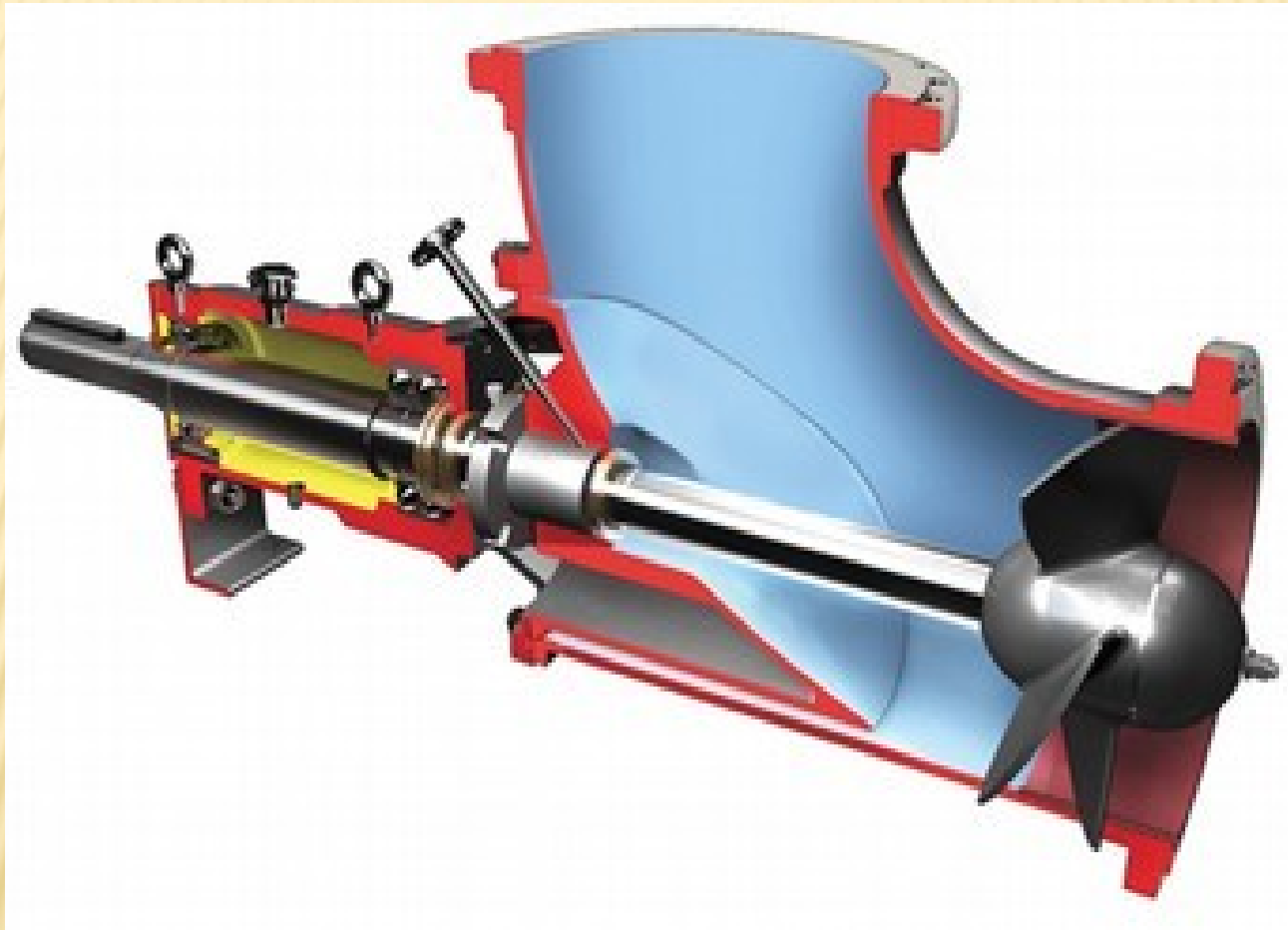
DIJAGONALNA PUMPA



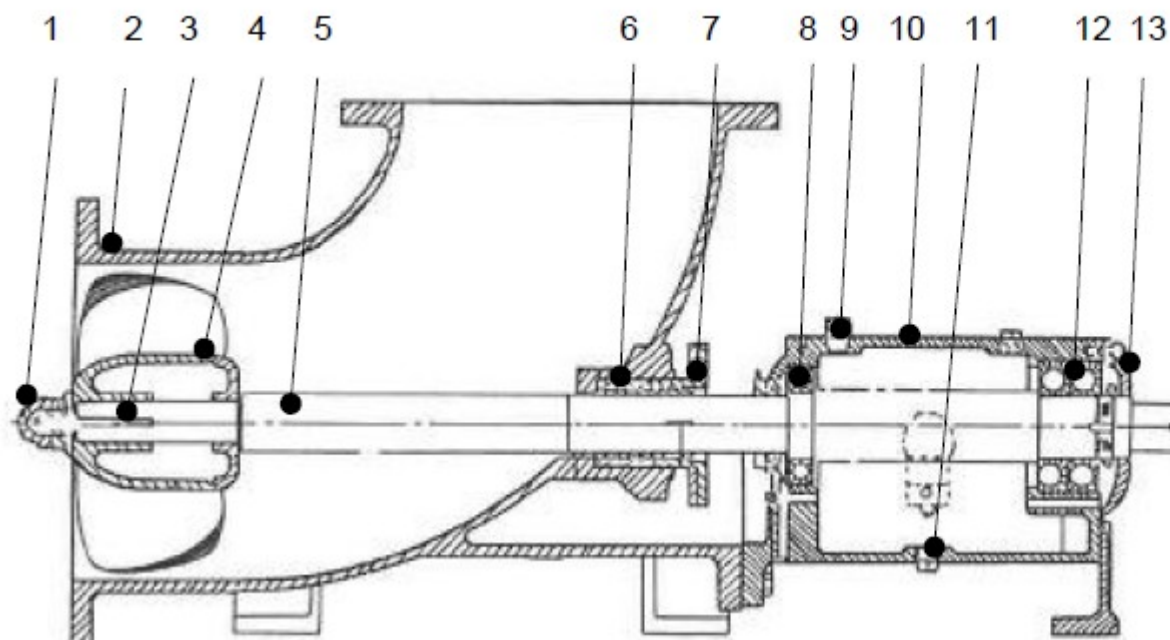
AKSIJALNA PUMPA - PROPELERNA



AKSIJALNA PUMPA - PROPELERNA



AKSIJALNA PUMPA - PROPELерна



- 1 Aerodinam. matica
- 2 Kućište pumpe
- 3 Klin
- 4 Rotor
- 5 Osovina
- 6 Brtva
- 7 Priteg brtve
- 8 Ležaj
- 9 Uljev ulja
- 10 Kućište ležaja
- 11 Ispust ulja
- 12 Ležaji
- 13 Stražnji poklopac